

# Solving Inverse Problems with Deep Learning

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# What is an Inverse Problem?

## Inverse Problems

Reconstruct a signal  $f \in \mathbb{R}^n$  from measurements

$$y \in \mathbb{R}^m, \quad y = A(f) + n,$$

where  $A$  is some (non-) linear measurement function and  $n$  is noise.

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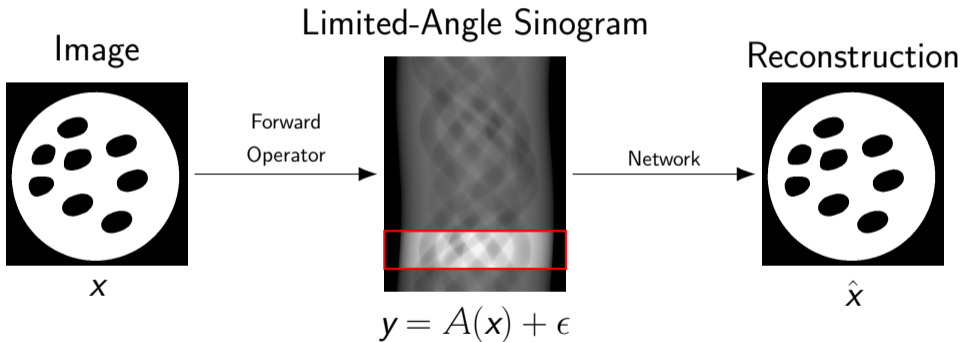
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Examples:

- Denoising, Deconvolution, Inpainting
- Limited-angle tomography, phase retrieval
- Very-long-baseline interferometry (VLBI) imaging
- And many more...

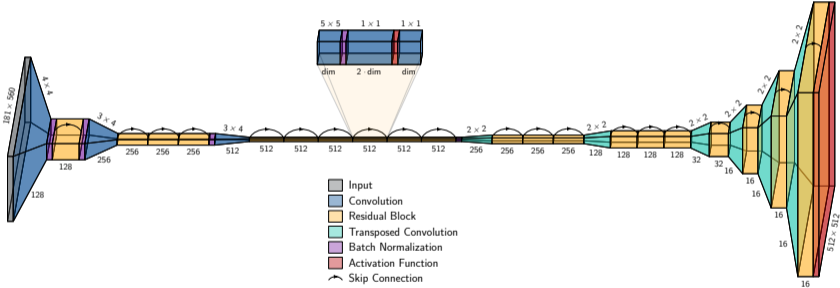
# Limited-Angle X-Ray Computed Tomography

**Team:** T. Germer, J. Robine, S. Konietzny, S. Harmeling, T. Uelwer



# End-to-end Learning on Synthetic Data for CT Reconstruction [1]

- Step 1** Generate synthetic images
- Step 2** Simulate sinograms from images using ASTRA [2]
- Step 3** Train reconstruction network for sinograms of similar images



9: KGq Cqy>pb4SCT>Vb^Szx ^%r>O-q CS'L r>} CY.Cqyi XS SC@Q^LYCzb\ bLq eP%qC-b^szq-<S^ fS @Ce C^@QbQ^@YC q'SL b^ s%zPCs:  
@-z i , eeYK@[ -zPC -zSs Hhql b@Cq^ ; P-YC'LCsi |C{

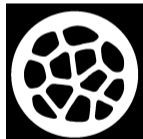
9: „ S. f^ , -qC„ SYC T^ d-YC'sSj>TCpC^ ; -^zB^SCT^ssC^s>GbYq 3YS Pp@>, ^@qS?- 4q fbYV>T^ ? C3CC^Pb-...Cq Vi Tbsz  
3-zC^4-q>- ^@T^ rSACpsi G-sz - ^@•CfSYC† Q%zb\ bLq eP%osSL zPC, ryp, zbbYbji a ezSs Bteqfss>|Jf||g|Ic|\_Q|IcJu>|CEv

# End-to-end Learning on Synthetic Data for CT Reconstruction [1]

Limited angle  
sinogram



Limited angle  
reconstruction



Error to  
ground truth



# Distributed Acoustic Sensing (DAS)

**Team:** S. Konietzny, V.H. Lai, T. Uelwer, M. Miller, J. Townsend, S. Harmeling

Measures ground motion as **strain rates** in the direction of a **fiber-optic cable**



Haast Pass Highway, New Zealand.

# Distributed Acoustic Sensing (DAS)

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Measures ground motion as **strain rates** in the direction of a **fiber-optic cable**

- **Backscattered light pulses** are sent through the cable
- Observe **change in particle displacements** along the cable



Haast Pass Highway, New Zealand.



# Distributed Acoustic Sensing (DAS)

DAS recording of an M7 earthquake.

# Distributed Acoustic Sensing (DAS)

Tasks:

- Remove coherent and incoherent noise
- Recover the underlying earthquake signal

Unlabeled data: evaluation relies on **synthetic data**

DAS recording of an M7 earthquake.

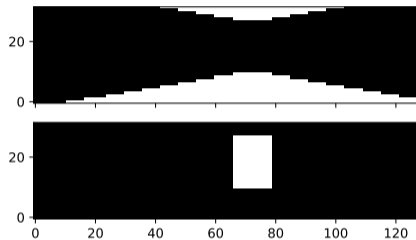
# Denoising DAS Data using Self-Supervised Learning

Current approach is based on Noise2Self [3]:

- Define fixed **hourglass masks**  $\setminus_P$  that can only process earthquake signals
- Predicting vehicle signals in **center regions**  $\setminus_<$  using only region masked by the hourglass masks is not possible
- Minimize

$$E_{(\setminus_<, \setminus_P)} \setminus_< \cdot (L_{\theta}(\setminus_P \cdot \hat{f}) - \hat{f}) \Big|, \quad (1)$$

where  $L_{\theta}$  is a parameterized function



Example  $32 \times 128$  **hourglass mask**  $\setminus_P$  (top) and its corresponding **center mask**  $\setminus_<$  (bottom).

**Thank you for your attention! Questions?**

- [1] Thomas Germer, Jan Robine, Sebastian Konietzny, Stefan Harmeling, and Tobias Uelwer. Limited-angle tomography reconstruction via deep end-to-end learning on synthetic data. *IEEE Transactions on Medical Imaging*, pages 0--0, 2023.
- [2] Wim van Aarle, Willem Jan Palenstijn, Jeroen Cant, Eline Janssens, Folkert Bleichrodt, Andrei Dabrovolski, Jan De Beenhouwer, K. Joost Batenburg, and Jan Sijbers. Fast and flexible X-ray tomography using the ASTRA toolbox. *IEEE Transactions on Medical Imaging*, 24(22):25129--25147, 2016.
- [3] Joshua Batson and Loïc Royer. Noise2self: Blind denoising by self-supervision. *arXiv preprint arXiv:1901.11365*, 2019.